

$$S = \frac{7\sqrt{3}}{16} - \frac{2}{3}$$